

# MA153 Lesson 45

## LESSON 45 - Surface Integrals

14 November, 2008

# Outline

- 1 Admin
- 2 Last Class
- 3 Surface Integrals
  - Course Guide
  - Definitions and Derivations
  - Homework Help
- 4 Look Forward

# Admin

1 This Week - Surface Integrals.

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- 2 Next Week - Project Drop on Monday, Stoke's Theorem on Tuesday and Wednesday, Divergence Theorem on Wednesday and Thursday, Guest Lecture on Friday: Dr. Ben Cole - Thayer 144 - Dean's Hour!

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- 3 Quiz, Today - You will have 10 Minutes!
- 4 Homework 8 due next Friday, 21 November!

# Block IV - Chapter 16

- 1 Vector Fields - 16.1: Functions that assign vectors to points in space.
- 2 Line Integrals - 16.2: Integrating over a curve.
- 3 Fundamental Theorem for Line Integrals - 16.3: Using FTC for line integrals.
- 4 Green's Theorem - 16.4:
- 5 Curl and Divergence - 16.5:
- 6 Parametric Surfaces and their Area - 16.6:

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- 9 Divergence Theorem - 16.9:

# Parametric Surface

1

$$\vec{r}(u, v) = x(u, v)\hat{i} + y(u, v)\hat{j} + z(u, v)\hat{k}$$

# Tangent Planes

1

$$\vec{r}_v = \frac{\partial x}{\partial v}(u_0, v_0)\hat{i} + \frac{\partial y}{\partial v}(u_0, v_0)\hat{j} + \frac{\partial z}{\partial v}(u_0, v_0)\hat{k}$$

$$\vec{r}_u = \frac{\partial x}{\partial u}(u_0, v_0)\hat{i} + \frac{\partial y}{\partial u}(u_0, v_0)\hat{j} + \frac{\partial z}{\partial u}(u_0, v_0)\hat{k}$$

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2

$$\vec{n} = \vec{r}_u \times \vec{r}_v$$

# Tangent Planes

1

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$$\vec{r}_u = \frac{\partial x}{\partial u}(u_0, v_0)\hat{i} + \frac{\partial y}{\partial u}(u_0, v_0)\hat{j} + \frac{\partial z}{\partial u}(u_0, v_0)\hat{k}$$

2

$$\vec{n} = \vec{r}_u \times \vec{r}_v$$

3

$$\vec{n} \cdot (\vec{r} - \vec{r}_0) = 0$$

# Surface Area

1

$$A(S) = \iint_D |\vec{r}_u \times \vec{r}_v| dA$$

# Surface Area

1

$$A(S) = \iint_D |\vec{r}_u \times \vec{r}_v| dA$$

2

$$A(S) = \iint_D \sqrt{1 + \left(\frac{\partial z}{\partial x}\right)^2 + \left(\frac{\partial z}{\partial y}\right)^2} dA$$

## Homework Help

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## Course Guide

### Surface Integrals - 16.7

- 1 Develop an understanding of the surface integral of a scalar functions viewed as and extension of the surface area integral.
- 2 Develop an understanding of oriented surfaces and positive orientation.
- 3 Determine the surface integral over a surface.
- 4 Develop an understanding of flux (surface integrals of vector fields).
- 5 Use surface integrals to determine the electric flux, net charge, and heat flow across a solid region.
- 6 **HOMEWORK PROBLEMS: 2, 10, 25**

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1 We are going to look in the book

# Board Work

- 1 A few problems to get you warmed up!

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# Look Forward

## Stokes' Theorem - 16.8

- 1 Understand how Stokes' Theorem relates surface integrals to line integrals around a boundary curve.
- 2 Be able to apply Stokes' Theorem.
- 3 **HOMEWORK PROBLEMS: 3, 8**

# Questions?

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